

5.3 (Part 2)

Horizontal Translations!

Turn to page 319 and have
[desmos.com](https://www.desmos.com) ready.

PROBLEM 2 Horizontal Translations



Consider the three exponential functions shown, where $h(x) = 2^x$ is the basic function.

- $h(x) = 2^x$
- $v(x) = 2^{(x+3)}$
- $w(x) = 2^{(x-3)}$

In Problem 1 *Vertical Translations*, the operations that produced the vertical translations were performed on the function $h(x)$. That is, 3 was added to $h(x)$ and 3 was subtracted from $h(x)$. In this problem, the operations are performed on x , which is the *argument* of the function. The **argument of a function** is the *variable* on which the function operates. So, in this case, 3 is added to x and 3 is subtracted from x .

You can write the given functions $v(x)$ and $w(x)$ in terms of the basic function $h(x)$. To write $v(x)$ in terms of $h(x)$, you just substitute $x + 3$ into the argument for $h(x)$, as shown.

$$h(x) = 2^x$$

$$v(x) = h(x + 3) = 2^{(x+3)}$$

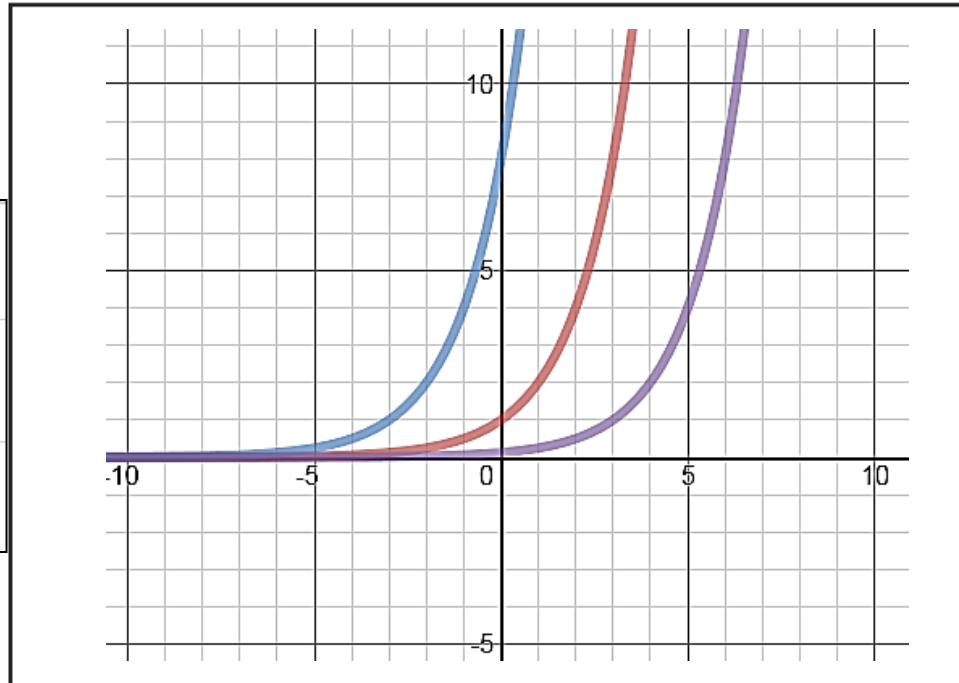
So, $x + 3$ replaces the variable x in the function $h(x) = 2^x$.

1. Write the function $w(x)$ in terms of the basic function $h(x)$.

$$w(x) = h(x - 3) = 2^{(x-3)}$$






2. Use a graphing calculator to graph each function with the bounds $[-10, 10] \times [-10, 10]$. Then, sketch the graph of each function. Label each graph.



Sketch the graphs one at a time to help you see which is which.



1	 $h(x) = 2^x$
2	 $v(x) = 2^{(x+3)}$
3	 $w(x) = 2^{(x-3)}$

3. Compare the graphs of $v(x)$ and $w(x)$ to the graph of the basic function. What do you notice? This is tricky!!! Look carefully.

The graph of $v(x)$ is shifted to the left 3 units, and the graph of $w(x)$ is shifted to the right 3 units.

4. Write the x-value of each ordered pair for the three given functions. You can use your graphing calculator to determine the x-values.

Go back to your graphs on desmos and use the "table" feature to find your x-values.

$h(x) = 2^x$	$v(x) = 2^{(x+3)}$	$w(x) = 2^{(x-3)}$
$(\underline{-2}, \frac{1}{4})$	$(\underline{-5}, \frac{1}{4})$	$(\underline{1}, \frac{1}{4})$
$(\underline{-1}, \frac{1}{2})$	$(\underline{-4}, \frac{1}{2})$	$(\underline{2}, \frac{1}{2})$
$(\underline{0}, 1)$	$(\underline{-3}, 1)$	$(\underline{3}, 1)$
$(\underline{1}, 2)$	$(\underline{-2}, 2)$	$(\underline{4}, 2)$
$(\underline{2}, 4)$	$(\underline{-1}, 4)$	$(\underline{5}, 4)$

Why are there no negative y-values given in this table?
HINT: You learned about it in the previous lesson!



5. Use the table to compare the ordered pairs of the graphs of $v(x)$ and $w(x)$ to the ordered pairs of the graph of the basic function $h(x)$. What do you notice?

For the same y-coordinate, the x-coordinate of $v(x)$ is 3 less than $h(x)$ and the x-coordinate of $w(x)$ is 3 more than $h(x)$.

A **horizontal translation** of a graph is a shift of the entire graph left or right. A horizontal translation affects the x-coordinate of each point on the graph.

You can use the coordinate notation shown to indicate a horizontal translation.

Turn to Page 321, #7.

7. Describe each graph in relation to its basic function.

a. Compare $f(x) = b^{x-c}$ to the basic function $h(x) = b^x$ for $c > 0$.

The graph of $f(x)$ is c units to the right of the graph of $h(x)$.

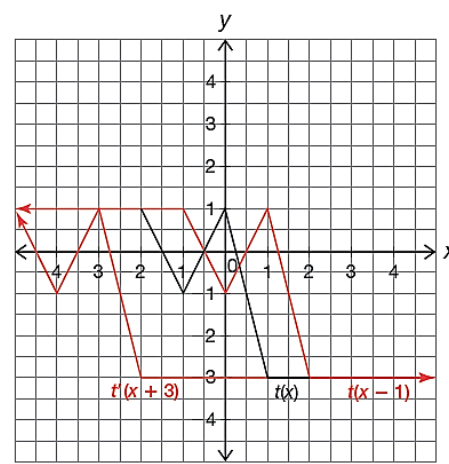
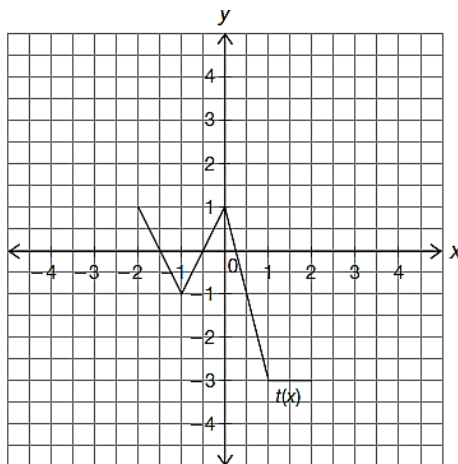
b. Compare $f(x) = b^{x-c}$ to the basic function $h(x) = b^x$ for $c < 0$.

The graph of $f(x)$ is c units to the left of the graph of $h(x)$.

8. The graph of a function $t(x)$ is shown. Sketch the graphs of $t'(x)$ and $t''(x)$.

a. $t'(x) = t(x + 3)$

b. $t''(x) = t(x - 1)$



Skip to the table on page 326.

Complete the table by describing the graph of each function as a transformation of its basic function.

Function Form	Equation Information	Description of Transformation of Graph
$f(x) = (x) + b$	$b > 0$	Vertical shift up b units.
	$b < 0$	Vertical shift down b units.
$f(x) = (x - b)$	$b > 0$	Horizontal shift right b units.
	$b < 0$	Horizontal shift left b units.
$f(x) = b^x + k$	$b > 1, k > 0$	Vertical shift up k units.
	$b > 1, k < 0$	Vertical shift down k units.
$f(x) = b^{x-c}$	$b > 1, c > 0$	Horizontal shift right c units.
	$b > 1, c < 0$	Horizontal shift left c units.

